

V.7 EOM in state-space form

$$x = \begin{bmatrix} z \\ \dot{z} \\ \theta \\ \dot{\theta} \end{bmatrix} \quad u = \tau \\ y = \begin{bmatrix} z \\ \theta \end{bmatrix}$$

From V.5

$$\ddot{z} = \ddot{z}$$

$$\ddot{\theta} = \ddot{\theta}$$

$$\ddot{z} = -\frac{5}{7}g\ddot{\theta}$$

$$\ddot{\theta} = \frac{1}{\frac{1}{3}m_2 l^2 + m_1 z_e^2} (-m_1 g \ddot{z} + l \tilde{F})$$

$$\begin{bmatrix} \ddot{z} \\ \ddot{\theta} \\ \ddot{z} \\ \ddot{\theta} \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & -\frac{5}{7}g & 0 & 0 \\ \frac{-m_1 g}{\frac{1}{3}m_2 l^2 + m_1 z_e^2} & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} z \\ \dot{z} \\ \theta \\ \dot{\theta} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{l}{\frac{1}{3}m_2 l^2 + m_1 z_e^2} \end{bmatrix} \tau$$

$$y = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} z \\ \dot{z} \\ \theta \\ \dot{\theta} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \end{bmatrix} \tau$$

7/17/17